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The Effect of Unions on Productivity in the Public Sector: The Case of Municipal Libraries

Ronald G. Ehrenberg  
Cornell University, rge2@cornell.edu

Joshua L. Schwarz  
Cornell University

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The Effect of Unions on Productivity in the Public Sector: The Case of Municipal Libraries

Abstract
[Excerpt] This paper represents our initial efforts at analyzing the effects of unions on productivity in the public sector. We first sketch an analytical framework that can be used to estimate these effects, focusing for expository purposes on municipal public libraries. We initially focus on libraries because considerable effort has been devoted to conceptualizing productivity measures for them and because of the availability of data to implement the framework. After discussing the analytical framework, we present preliminary estimates of the effects of unions on productivity in public libraries based upon analyses of data from 71 municipal libraries in Massachusetts. We conclude by indicating how these analyses will be extended and the direction that we hope our future research will take.

Keywords
unions, productivity, public sector, libraries, Massachusetts

Disciplines
Labor Economics | Labor Relations | Library and Information Science | Unions

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THE EFFECT OF UNIONS ON PRODUCTIVITY IN THE PUBLIC SECTOR: THE CASE OF MUNICIPAL LIBRARIES

Ronald G. Ehrenberg and Joshua L. Schwarz

I. Introduction

Research by economists on the economic effects of unions in the private sector has tended to focus on unions' effects on their members' relative earnings positions. Following in the tradition of H.G. Lewis' pioneering work, a large number of studies have addressed this question. The more sophisticated ones use micro-level data and seek to control both for quality differentials and the possibility that wages and union status may be simultane-

EHRENBERG is Professor of Economics and Labor Economics and SCHWARZ is a graduate student at the New York State School of Industrial and Labor Relations at Cornell University.

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eously determined. Most recently, other non-wage outcomes, such as job satisfaction and labor turnover, have been considered and analysts have attempted to ascertain if part of any observed union/nonunion wage differential merely compensates unionized employees for relatively unfavorable nonpecuniary conditions of employment.

The traditional neoclassical view of unions asserts that although unions may benefit their members by creating noncompensating wage differentials, they cause allocative efficiency losses. Hence, their net impact on the economy

\[\text{References}\]


as a whole is thought to be negative. Recently, however, this view has been challenged by Richard Freeman, James Medoff, and their associates at Harvard. Drawing on hypotheses put forth long ago by institutional economists, they argue that unions may well increase productivity. Such increases may occur through a number of routes including union-induced reductions in turnover, increases in morale and motivation, and increases in formal and informal on-the-job training. Indeed, several of their econometric studies suggest that union/nonunion productivity differentials in the private sector are often positive. To the extent that these results are generalizable, one must be-

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4See, for example, Albert Rees, The Economics of Work and Pay, 2nd ed. (New York, Harper and Row, 1979), chapter 10, for a summary of the neoclassical view, which does not necessarily represent his personal view.

5A good nontechnical treatment of their views is found in Richard Freeman and James Medoff, "The Two Faces of Unionism," Public Interest (Fall 1979).

come much more agnostic on the question of whether unions in the private sector have had net adverse efficiency effects.

Research on the effects of unions in the public sector has paralleled the private sector studies. Numerous studies have sought to ascertain the effect of public sector unions on the relative wages of teachers, police, firefighters and other categories of municipal employees.\(^7\) Recent studies have moved beyond wage effects and analyzed the effects of public sector unions on nonwage employee benefits and on the trade-off between wages and retirement system characteristics.\(^8\)

In contrast to the private sector research, however, no research has been directed towards ascertaining the effects of unions on productivity in the public sector. This fact is not completely surprising; the concepts of output and productivity in the public sector


are often not well-defined and the difficulties inherent in trying to measure productivity are consequently large. Nevertheless, the growing financial problems of state and local governments suggest that this important problem cannot be ignored. Prior studies of public sector wage determination have indicated, on average, that unions have tended to have only modest effects on their members' compensation; studies of public employees unions' effects on productivity are required to complete our understanding of the effects these unions have had on municipal finances and service flows.

This paper represents our initial efforts at analyzing the effects of unions on productivity in the public sector. We first sketch an analytical framework that can be used to estimate these effects, focusing for expository purposes on municipal public libraries. We initially focus on libraries because considerable effort has been devoted to conceptualizing productivity measures for them and because of the availability of data to implement the framework. After discussing the analytical framework, we present preliminary estimates of the effects of unions on productivity in public libraries based upon analyses of data from 71 municipal libraries in Massachusetts. We conclude by indicating how these analyses will be extended and the direction that we hope our future research will take.

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II. A Simple Analytic Framework

Municipal libraries produce a variety of outputs which include, but are not limited to, the circulation of books, periodicals, and other audio-visual materials, responding to information and inter-library loan requests, and providing reference facilities. These outputs can, in theory, be evaluated in both quantitative and qualitative ways. While one can simply count circulation figures or the number of information requests, more sophisticated valuations of library output would focus on questions like: What proportion of information requests were answered correctly? or, How long did the typical borrower have to wait for a book that he or she wanted?

For now we shall ignore the fact that libraries can be thought of as multiple product firms and also ignore the quality dimension of the services they provide. Instead, we assume that we can treat library output \( Q \) as being a single variable. One can then specify the community demand function for library services by

\[
D = D(P | V_1, V_2)
\]

Here \( P \) is the "price" the community must pay for a unit of library services; other things being equal, the higher the price the less library services will be demanded. The position of the demand curve will depend upon community income or wealth, with higher income areas demanding more library services, and it will also obviously depend upon the size of the community \( V_1 \). Finally, the demand curve will depend upon the community's "taste" for library services \( V_2 \). For example, more highly educated communities may demand more library services, as may communities with a large proportion of school-age children.
The second element of our model is a production function for library services.

\[ Q = F(K,L|V_3,U) \]

Here we have treated output, capital (K) and labor (L) as single variables. The capital stock includes the library's entire stock of materials as of the current period. \( V_3 \) is a vector which represents those community variables that affect the position or shape of the production function. For example, one early study found that two-thirds to three-quarters of all library users lived within one mile of a library.\(^{10}\) This suggests that increases in population density, which make it easier to locate branch libraries within a mile of all individuals, would increase the output of library services, ceteris paribus.

The production function for library services may also be a function of whether the library's employees are represented by a union. As noted by Freeman and Medoff, unionization (U) may well increase productivity through routes including union-induced reductions in turnover, increases in morale and motivation, and increases in formal and informal on-the-job training.\(^{11}\) On the other hand, unionization of library employees may well reduce productivity if it places limits on library management's ability to substitute factors of production or if it requires library management to devote more resources to the contract negotiation pro-


\(^{11}\) Freeman and Medoff, "The Two Faces of Unionism," *Public Interest*, Fall 1979.
cess and to the resolution of grievances. Of key concern to us is what is the net effect of unions on the production function?

The stock of capital that a library has depends upon its stock of capital in the preceding period ($K_{-1}$), its investment in new capital (I), and the rate at which its previous stock of capital depreciates ($\delta$). The latter depends upon the age distribution of the library's books (in the main, books are used most heavily in the initial years following their purchase) and the resources that the library devotes to maintaining its collection and avoiding theft. We shall ignore the latter two considerations here and treat the depreciation rate as a constant.

\[ K = I + (1-\delta)K_{-1} \]

The costs incurred by a library are primarily for labor, for new acquisitions, and for maintaining the library's collection and buildings. Let $W$ be the cost per unit of labor, $m$ the per unit cost of maintaining the collection, and $C$ the user cost of new materials. Then the total costs the library incurs is given by

\[ C = WL + CI + mK_{-1} \]

For later reference, remember that a primary goal of unions is to increase their members'

---

wages. To the extent that they are successful, \( W \) will be an increasing function of \( U \).

The cost function for library services is obtained by minimizing (4), subject to (2) and (3). From this, one can obtain the average cost function for library services

\[
AC = AC(Q|W,C,m,V_3,δ,K_{-1}F,U)
\]

If the underlying library production function exhibits constant (decreasing) (increasing) returns to scale, average cost will be constant (increase with output) (decrease with output).

We have plotted the demand curve and average cost curve for library services in Figure 1, the latter under the assumption of constant average costs. The average cost curve represents the price to the library of producing different levels of library services. Given the demand curve, \( D \), \( Q^* \) units of library services will be demanded and produced. At this level of library services, library revenues just cover its costs.

The equilibrium level of library services can be expressed as the reduced form equation

\[
Q^* = G(V_1, V_2, V_3, W, C, m, δ, K_{-1}, F, U)
\]

Obviously, anything that shifts the demand curve up will increase output while anything that shifts the average cost curve up will reduce it. The key point to note is that observed output is determined by both demand and cost factors.

The effects of unions on service flows operate both via their effects on wages and their effects on the production function (2). If unions do increase the wages of library
Figure 1
The Market for Library Services
employees this would shift the average cost curve up and reduce output. If unions increase (decrease) the level of output associated with any given input levels (for the reasons discussed earlier) this will shift the average cost curve down (up), thereby increasing (decreasing) output.

Equation (6) provides a simple framework which can be used to estimate the effects of unions on productivity. If cross-section data on library services, the demand and cost variables, and unionization can be obtained, the model can be implemented. The coefficient of the unionization variable in this model would represent the net effect of library unions on productivity. If one were to estimate (6) omitting the wage variable, however, the coefficient of the unionization variable would capture both the net effect of unions on the production function for library services and the effect of union-induced wage gains on average costs and, hence, output.

III. Extensions of the Framework

The simple framework sketched above may be inadequate for a number of reasons. First, the wage of library employees is endogenous, in the sense that it will be determined both by whether the library employees are unionized and the forces that affect the demand for library services, as well as other variables \( V_4 \).\(^{13}\) As such, if one were to specify a wage determination equation of the form

\[
W = W(V_1, V_2, V_4, U),
\]

\(^{13}\) For a discussion of the variables that influence public sector wage determination, see Ehrenberg and Goldstein, op. cit.
it is likely that the error term in this equation would be correlated with the error term in (6). This might happen, for example, if data on some variable that affected the demand for library services was unavailable and omitted from both equations (6) and (7). If correlated error terms occurred, biased estimates of (6) would result if it was estimated by ordinary least squares.

Second, the extent of unionization, as measured by whether a library's employees are covered by a collective bargaining agreement, is also likely to be endogenously determined. It is not unreasonable to expect that collective bargaining coverage will be a function both of state laws governing public employee unionization and the proportions of public and private employees in a state that are union members. The size of the library is also likely to matter; large libraries may be more bureaucratic in nature and more conducive to unionization. Finally, collective bargaining coverage is likely to be related to both the estimated wage premium associated with collective bargaining and the estimated productivity differential associated with collective bargaining; the former because it influences both employees' demand for collective bargaining coverage and library management's resistance to it, the latter because the productivity effects associated with collective bargaining also influence management's resistance to it.

This suggests the need for a full-blown "selectivity bias" corrected model. Separate wage and library output equations can be estimated for libraries covered by and not covered


15 See Lung-Fei Lee, op. cit., for the genesis of this approach.
by union contracts, in the context of a model in which the probability that a library is unionized is determined by the estimated union/nonunion wage and output differentials that exist for it, as well as other explanatory variables. The appendix traces out formally how this can be done.

Third, the analyses described above focuses on the effect of unions on observed output; the latter is determined by both demand and cost considerations. One might prefer instead to focus directly on the underlying production process for library services and ask questions like: Does the existence of unions alter library output per employee? Do unions affect the substitutability of capital for labor in the provision of library services? Or shifting to the case of multiple types of library employees (e.g., librarians, other professional employees, library aides, other clerical employees): Do unions alter the substitutability of different categories of library employees in the face of relative price changes? Such generalizations would involve using a variant of the "production function" approach used by Brown and Medoff, and Clark, and/or estimating the parameters of a production function from cost share data.

For example, if the production function for library service in equation (2) can be written as

\[ Q = AK^u [L(1+BU)]^{1-a} \]

where B represents the proportionate marginal productivity differential of union labor, and U equals one if the library is unionized and zero otherwise, then

\[ \log(\frac{Q}{L}) = \log A + a\log(K/L) + (1-a)BU \]

Hence, regressing the log of output per library employee on those demographic variables that
affect library productivity (variables that underlie A), the log of the capital/labor ratio, and whether the library is organized would enable one to estimate the proportionate marginal productivity advantage of union labor. The extension to allow for nonconstant returns to scale or more than one category of labor is straightforward in this model. To test for union effects on substitutability, however, obviously requires more flexible functional forms such as the CBS or translog ones.

IV. Preliminary Empirical Results: The Determinants of Productivity in Massachusetts Public Libraries

In 1977 the International City Management Association (ICMA) conducted a survey of municipal public libraries, obtaining data on library revenues and expenditures, employment and wage scales for different categories of library employees, the number of books in each library, and various measures of library usage including circulation, borrowers, and interlibrary loans. The latter three variables were published, by library, in the 1978 Municipal Yearbook, and when coupled with published data on socioeconomic characteristics of cities obtained from the 1977 City and County Databook and published data on whether any library employees were covered by a collective bargaining agreement in each Massachusetts municipality in 1977, permit us to estimate equations of the form

\[ Q_{ki} = \sum_{j=1}^{10} B_{kj} r_{ji} + \gamma_k u_i + \varepsilon_{ki} \]

\[ K = 1, 2, 3, 4, 5 \]

for a sample of 71 municipal libraries.

16 See Brown and Medoff, op. cit.
Equation (10) is a condensed version of the reduced form library output equation (6) derived in Section II. The output measures available are interlibrary loans per capita \( (Q_1) \), number of borrowers per capita \( (Q_2) \), circulation per capita \( (Q_3) \), interlibrary loans per borrower \( (Q_4) \), and circulation per borrower \( (Q_5) \), each measure expressed in natural logarithm form. The former three measures may be thought of as measures of total services provided, while the latter two may be regarded as measures of the quantity of services provided per library user.

The \( r_i \) are those variables that are expected to influence library output, either from the demand or cost sides of the model. The cost side is captured here by population density \( (r_1) \); as noted earlier, previous studies have suggested that increased population density reduces the cost of providing library services, and hence should increase library output. The demand side is represented by a set of variables expected to influence a community's preferences for library services; these include the percent of the population that is female \( (r_2) \), the percent nonwhite \( (r_3) \), the percents of the population that are older than age 18 \( (r_4) \) and age 65 \( (r_5) \), the median education level in the community \( (r_6) \), the female labor force participation rate \( (r_9) \), and the fraction of employees in the municipality employed in education \( (r_{10}) \). The demand side also is represented by the community's capacity to pay for library services, as measured by the median family income \( (r_7) \), and per capita intergovernmental revenues \( (r_8) \). Finally, \( U_i \) as a dichotomous variable indicating whether any library employees in the municipality were covered by a collective bargaining agreement in 1977.
Several things should be noted about this specification. Data limitations in this initial study preclude a number of variables that appear in equation (6) from appearing in equation (10). The omitted variables include the wage rates of library employees, the lagged stock of library materials, and the rate at which library materials depreciate. The estimated coefficients which we report below should be considered very tentative then; they may well suffer from omitted variable bias. In particular, because library employees' wages were unavailable in this sample, the coefficient of the unionization variable will capture both the net effects of collective bargaining on the production function for library services and of union induced wage gains on average costs and hence output.

Our preliminary estimates of equation (10) appear in Table 1. The populations of the municipalities in our sample varied from 10,000 to over 500,000, and to control for heteroscedasticity we have weighted each observation by the square root of its population. The employees were covered by a collective bargaining agreement in approximately one-quarter of the libraries in the sample.

Turning first to the vector of variables other than unionization, many of these variables affect library output in a manner consistent with our a priori predictions. An increase in the school age population (decrease in \( r_4 \)) increases library usage as does an increase in the proportion of the population over age 65 (\( r_5 \)). An increase in the median education level of the population (\( r_6 \)) also leads to higher usage, as does an increase in the proportion of employees who are employed in the education industry (\( r_{10} \)).
Table 1
Determinants of Productivity in Massachusetts Public Libraries in 1977: Weighted Least Squares
(absolute value t statistics)

<table>
<thead>
<tr>
<th>Ind./Dep. Var./Var.</th>
<th>$Q_1$</th>
<th>$Q_2$</th>
<th>$Q_3$</th>
<th>$Q_4$</th>
<th>$Q_5$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_1^a$</td>
<td>-.111 (3.0)</td>
<td>-.056 (4.3)</td>
<td>-.066 (7.1)</td>
<td>-.059 (1.6)</td>
<td>-.009 (0.8)</td>
</tr>
<tr>
<td>$r_2$</td>
<td>-.060 (0.6)</td>
<td>.090 (2.6)</td>
<td>-.004 (0.2)</td>
<td>-.151 (1.6)</td>
<td>-.094 (2.8)</td>
</tr>
<tr>
<td>$r_3$</td>
<td>.138 (2.1)</td>
<td>.041 (1.8)</td>
<td>.021 (1.3)</td>
<td>.097 (1.6)</td>
<td>-.020 (0.9)</td>
</tr>
<tr>
<td>$r_4$</td>
<td>-.138 (1.9)</td>
<td>-.021 (0.8)</td>
<td>-.067 (3.8)</td>
<td>-.117 (1.7)</td>
<td>-.045 (1.9)</td>
</tr>
<tr>
<td>$r_5$</td>
<td>.192 (1.6)</td>
<td>-.006 (0.1)</td>
<td>.127 (4.3)</td>
<td>.197 (1.7)</td>
<td>.132 (3.2)</td>
</tr>
<tr>
<td>$r_6^a$</td>
<td>.467 (2.0)</td>
<td>.173 (2.0)</td>
<td>.186 (3.1)</td>
<td>.313 (1.3)</td>
<td>.013 (0.2)</td>
</tr>
<tr>
<td>$r_7$</td>
<td>-.038 (0.5)</td>
<td>-.014 (0.5)</td>
<td>.015 (0.8)</td>
<td>-.023 (0.3)</td>
<td>.028 (1.2)</td>
</tr>
<tr>
<td>$r_8^a$</td>
<td>-.045 (0.0)</td>
<td>.094 (0.2)</td>
<td>.014 (0.0)</td>
<td>-.149 (0.1)</td>
<td>.080 (0.2)</td>
</tr>
<tr>
<td>$r_9$</td>
<td>.871 (1.2)</td>
<td>.879 (0.6)</td>
<td>.096 (2.1)</td>
<td>.752 (1.5)</td>
<td>2.975 (2.2)</td>
</tr>
<tr>
<td>$r_{10}$</td>
<td>3.566 (0.8)</td>
<td>2.139 (1.4)</td>
<td>4.668 (4.2)</td>
<td>1.427 (0.3)</td>
<td>2.529 (1.7)</td>
</tr>
</tbody>
</table>

$U = -.540 (1.5) \quad .256 (2.1) \quad -.128 (1.5) \quad -.797 (2.3) \quad -.385 (3.2)$

$R^2 = .334 \quad .515 \quad .731 \quad .235 \quad .417$

$a = -71$ for all equations
$s = \text{coefficient has been multiplied by 1000}$

and

$Q_1 = \log_e$ (interlibrary loans per capita)
$Q_2 = \log_e$ (number of borrowers per capita)
$Q_3 = \log_e$ (circulation per capita)
$Q_4 = \log_e$ (interlibrary loans per borrower)
$Q_5 = \log_e$ (circulation per borrower)

$r_1 = \text{population density}$
$r_2 = \text{percent female}$
$r_3 = \text{percent nonwhite}$
$r_4 = \text{percent of the population age 18 and over}$
$r_5 = \text{percent of the population age 65 and over}$
$r_6 = \text{median education level}$
$r_7 = \text{median family income}$
$r_8 = \text{per capita intergovernmental revenue}$
$r_9 = \text{female labor force participation rate}$
$r_{10} = \text{fraction of employees in education}$
In contrast, neither of the variables that reflect the communities' capacity to pay \( r_j \) and \( r_g \) are significantly related to library output. While an increase in the proportion of the population that is female \( r_j \) leads to an increase in the number of borrowers, a result that might be expected if females tend not to be in the labor force, an increase in the labor force participation rate of females \( r_g \) is associated with higher circulation of library materials. Finally, an increase in population density \( r_d \) leads to a reduction in library output and an increase in the proportion of the population that is nonwhite \( r_3 \) to higher output.\(^{17}\)

The primary variable of interest to us, of course, is the unionization variable. These data suggest that libraries covered by collective bargaining agreements have, ceteris paribus, some 29.2 \( [\exp(.256)-1] \) percent more borrowers per capita than do nonunion libraries. Both circulation and interlibrary loans per capita appear to be lower in unionized libraries; however, these effects are not significantly different from zero. Because of these results, it is not surprising that on a

\(^{17}\) Malcolm Getz, *Public Libraries: An Economic View*, finds a similar negative relationship between density and library output in his study of branch libraries in New York City. He argues that population density may be a proxy for the rental cost of structures, with more dense areas having higher rental rates. If this occurs, the average cost of library services may well be higher in denser areas which would lead, from Figure 1, to a lower level of library services. Thus, a negative relationship between population density and library output may well be consistent with our model.
per borrower basis, circulation and interlibrary loans are also lower in unionized libraries.\textsuperscript{18}

How robust are these results to the estimation methods used? Row (1) of Table 2 summarizes compactly the estimated collective bargaining effects from Table 1. Rows (2) and (3) show that estimates obtained are virtually identical when the method of ordinary least squares is used [row (2)] and when an additional variable, median age, is included to more fully control for the age distribution of the population [row (3)].

As noted in Section II, however, all of these estimates may well be subject to selectivity bias. Using the method described in the appendix, one can attempt to control for this problem.\textsuperscript{19} First, a reduced form probit equation is estimated that determines the probability that a library's employees are covered by a collective bargaining agreement. From these equations, one can compute estimates of variables which are then added to the productivity equations to control for the probability that a library's employees are covered by a collective bargaining agreement. These "augmented" productivity equations can then be estimated by ordinary least squares and consistent parameter estimates obtained; this is done separately for libraries that are covered by collective bargaining agreement and those that are not. Finally, the estimated parameters and the mean

\textsuperscript{18} Put another way, if an increase in a variable causes the log of $X_1$ to increase but does not affect the log of $X_2$, it is not surprising that the log of $(X_2/X_1)$ falls.

\textsuperscript{19} Actually, the method implemented here is simpler since it ignores library employees' wage rates.
Table 2

Estimated Effects of Collective Bargaining Coverage on the Logarithms of Library Output Measures: Various Estimation Methods and Model Specifications (absolute value t statistic)

<table>
<thead>
<tr>
<th>Dep. Speciﬁcation/Var.</th>
<th>Q1</th>
<th>Q2</th>
<th>Q3</th>
<th>Q4</th>
<th>Q5</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1)</td>
<td>-.540 (1.5)</td>
<td>.256 (2.1)</td>
<td>-.129 (1.5)</td>
<td>-.797 (2.3)</td>
<td>-.385 (3.2)</td>
</tr>
<tr>
<td>(2)</td>
<td>-.573 (1.7)</td>
<td>.252 (1.8)</td>
<td>-.140 (1.5)</td>
<td>-.825 (2.5)</td>
<td>-.393 (2.9)</td>
</tr>
<tr>
<td>(3)</td>
<td>-.535 (1.5)</td>
<td>.287 (2.2)</td>
<td>-.098 (1.0)</td>
<td>-.822 (2.3)</td>
<td>-.386 (2.8)</td>
</tr>
<tr>
<td>(4)</td>
<td>-.994</td>
<td>.186</td>
<td>-.277</td>
<td>-1.052</td>
<td>-.471</td>
</tr>
</tbody>
</table>

where (1) weighted least squares (union coeffcients from Table 1)
(2) ordinary least squares estimates - same model as in Table 1
(3) ordinary least squares estimates - median age added as an additional explanatory variable
(4) selectivity bias corrected estimates, separate equations estimated for union and nonunion sectors (see Appendix A)
values of the explanatory variables can be used to compute consistent estimates of the union/nonunion productivity differentials.

Estimates of the reduced form probit equation appear in Table 3. The variables that appear in the equation include those in the output equations as well as population size, population growth, and the share of employment in the city in a number of industries. These latter variables were included because they tend to be related to the extent of private sector unionization across SMSA's. While the vector of coefficients is clearly jointly significant at the .05 level, most of the individual coefficients are statistically insignificant. The few significant coefficients suggest that collective bargaining for library employees in Massachusetts tends to occur in cities with older populations ($r_5$), higher female labor force participation rate ($r_9$), and lower levels of service industry employment ($r_{15}$).

These estimates are then used, as described above, to obtain consistent estimates of the productivity equations and estimates of the union/nonunion productivity differentials. These differentials are summarized in row (4) of Table 2; in the main their pattern is very similar to the previous results.


21 For brevity, we do not report the regression coefficients for the "selectivity corrected" output equation here.
Table 3

Probit Estimates of Whether Any Library Employees Are Covered by a Collective Bargaining Agreement in 1977

(absolute value asymptotic t ratio)

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>17.499 (0.9)</td>
</tr>
<tr>
<td>$r_{1}$</td>
<td>.119 (0.9)</td>
</tr>
<tr>
<td>$r_{2}$</td>
<td>-.189 (0.6)</td>
</tr>
<tr>
<td>$r_{3}$</td>
<td>-.543 (1.0)</td>
</tr>
<tr>
<td>$r_{4}$</td>
<td>-.496 (1.7)</td>
</tr>
<tr>
<td>$r_{5}$</td>
<td>.541 (1.9)</td>
</tr>
<tr>
<td>$r_{6}$</td>
<td>.586 (0.9)</td>
</tr>
<tr>
<td>$r_{7}$</td>
<td>.116 (0.8)</td>
</tr>
<tr>
<td>$r_{8}$</td>
<td>3.081 (1.2)</td>
</tr>
<tr>
<td>$r_{9}$</td>
<td>30.363 (1.9)</td>
</tr>
<tr>
<td>$r_{10}$</td>
<td>.011 (0.1)</td>
</tr>
<tr>
<td>$r_{11}$</td>
<td>-.045 (0.6)</td>
</tr>
<tr>
<td>$r_{12}$</td>
<td>-.052 (0.4)</td>
</tr>
<tr>
<td>$r_{13}$</td>
<td>-.470 (1.6)</td>
</tr>
<tr>
<td>$r_{14}$</td>
<td>.151 (0.6)</td>
</tr>
<tr>
<td>$r_{15}$</td>
<td>.037 (1.4)</td>
</tr>
<tr>
<td>$r_{16}$</td>
<td>.273 (0.1)</td>
</tr>
<tr>
<td>$r_{17}$</td>
<td>.042 (0.2)</td>
</tr>
</tbody>
</table>

Log Likelihood -23.746

$X^{2}$ 32.313

$u$ 71

where $r_{11}$ fraction of employees in manufacturing

$r_{12}$ fraction of employees in transportation and public utilities

$r_{13}$ fraction of employees in the service industry

$r_{14}$ fraction of employees in construction

$r_{15}$ 1975 population

$r_{16}$ percentage population change 1960-1975

C intercept term

and

*Coefficient has been multiplied by 1000.
V. Extensions and Future Directions

This paper has laid out a methodological framework for estimating the effects of unions on productivity in the public sector and presented some preliminary estimates for a sample of 71 municipal public libraries in Massachusetts. The empirical estimates themselves should not be stressed, however, as the underlying data suffer from a number of weaknesses! First, there are numerous important variables omitted from the data set, including wages and employment levels of library employees, new acquisitions, and the stock of library materials; these omissions may seriously bias the estimated union effects. Second, we have not made a serious attempt to specify the determinants of whether a library is covered by a collective bargaining agreement; only a limited number of variables were entered into that equation and this could further bias our results. Finally, the libraries in our sample all are located in one state and span a wide range of city sizes (under 10,000 to over 500,000). Since libraries in cities of different sizes perform different functions and the likelihood of collective bargaining coverage is positively related to city size, this will further distort our findings.

We hope to get around all of these problems in future work. The ICMA has made the data tape, upon which their published report on municipal libraries was based, available to us. This tape provides fairly comprehensive data on all of the "library variables" needed to implement the various approaches discussed in Sections II and III for approximately 250 cities of population size 25,000 or greater. Socioeconomic characteristic variables for these cities can be obtained from the 1977 City and County Databook. Finally, we have obtained data on the collective bargaining coverage of
library employees in these cities by a mail survey; our response rate to this survey has been well over 90 percent.

Because these cities do not all lie in one state, it will be possible for us to better model the forces that affect the probability that library employees in a city are covered by a collective bargaining agreement. These include the extent of public and private unionization in a state, variables for which published data exist, as well as the laws governing public sector collective bargaining in a state. Our colleague, John Burton, has expended considerable effort to collect data on, and to define the parameters of, these laws and has generously made these data available to us. A substantially better specified probability of collective bargaining coverage equation should reduce the likelihood that our estimates of union productivity effects are subject to selectivity bias.

In addition to our more comprehensive analysis of the effect of unions on productivity in public libraries, we also plan to pursue the question of the routes by which unions influence productivity in the public sector. Our initial focus in this aspect of the project will be on public education and we will make use of a unique set of longitudinal data on educational outcomes, school district background variables, and union contract provisions that our colleague, Sam Bacharach, has constructed for local school districts in the state of New York. Our analyses here will permit us to test for the effects of specific union contract provisions on educational outcomes, rather than for the effects of collective bargaining coverage per se. The longitudinal nature of the data will permit the application of econometric
methods that allow one to control for omitted variables that otherwise might bias the analyses. In sum, these methods substantially reduce the likelihood that the estimates that result will be subject to selectivity bias because omitted variables that affect the probability of collective bargaining coverage or contract provisions may also affect educational outcomes.

22 For details, see Ronald G. Ehrenberg, "Unions and Productivity in the Public Sector" (proposal submitted to the National Science Foundation, March 1980).
Appendix

Our goal is to estimate whether libraries whose employees are union members are more, or less, productive than otherwise identical libraries whose employees are not union members, and to estimate the extent that unions increase library employees’ wages. Suppose that the output of library $i$ would be $Q_{ui}$ if its employees were covered by a collective bargaining agreement and $Q_{ni}$ if its employees were not covered by a collective bargaining agreement. Suppose also that the wages the library’s employees would receive in the two environments would be $W_{ui}$ and $W_{ni}$ respectively. Then we can define the relative output differential, $d_{q_i}$, and the relative wage differential, $d_{w_i}$, associated with collective bargaining for the $i^{th}$ library, as

\begin{align}
(Al) \quad d_{q_i} &= \frac{Q_{ui} - Q_{ni}}{Q_{ni}} = \log\left(\frac{Q_{ui}}{Q_{ni}}\right) \\
&= \frac{W_{ui} - W_{ni}}{W_{ni}} = \log\left(\frac{W_{ui}}{W_{ni}}\right)
\end{align}

In general, it is not possible to observe both $Q_{ui}$ and $Q_{ni}$, or $W_{ui}$ and $W_{ni}$ with cross-section data, as at a point in time either a library’s employees are covered by an agreement or they are not. A naive approach that circumvents this problem is to estimate wage and output equations separately for employees in cities with and without agreements, use the estimated coefficients from these regressions and the characteristics of a city to compute predicted values of the wage and library output that would be observed in both sectors, and then estimate the differentials by calculating the percentage difference in these predicted values.
More formally, suppose that we postulate that the wage rate library employees would receive in a city if they are unionized is a log linear function of a vector of variables, \( \mathbf{X} \), which represent all of the variables that would appear in equation (7) in the text, plus a random error term \( \varepsilon_{1i} \)

\[
\text{(A2)} \quad \log W_{ui} = \sum_{j=1}^{K} a_{ju} x_{ju} + \varepsilon_{1i}
\]

and that a similar functional relationship exists that describes the wage that library employees would receive in a city if they were not unionized.

\[
\text{(A3)} \quad \log W_{ni} = \sum_{j=1}^{K} a_{jn} x_{ji} + \varepsilon_{2i} \cdot
\]

Suppose also that similar output equations could be derived; these correspond to the reduced form output equation (6) in the text, where the \( Y_{ji} \) represent all of the variables in equation (6) save the extent of unionization, and \( \varepsilon_{3i} \) and \( \varepsilon_{4i} \) are random error terms

\[
\text{(A4)} \quad \log Q_{ui} = \sum_{j=1}^{M} B_{ju} Y_{ji} + \varepsilon_{3i}
\]

\[
\text{(A5)} \quad \log Q_{ni} = \sum_{j=1}^{M} B_{jn} Y_{ji} + \varepsilon_{4i} \cdot
\]

The naive approach would involve estimating the parameters of (A2) and (A4) by ordinary least squares from observations on libraries whose employees were unionized and the parameters of (A3) and (A5) by ordinary least squares from observations on libraries whose employees were not organized. Given estimates of these parameters \( \hat{a}_{ju}, \hat{a}_{jn}, \hat{B}_{ju}, \hat{B}_{jn} \) and the relevant characteristics of a representative city \( (X_{ji}, Y_{ji}) \), one can then obtain estimates of the relative output and wage differentials from
As is now well-known, however, estimates of wage and output equations from truncated samples will not necessarily yield unbiased estimates of the parameters of the underlying wage and output equations (and hence $\hat{d}_{qi}$ and $\hat{d}_{ui}$) since the assumption that the error term in each equation is random and uncorrelated with the other explanatory variables is typically violated. This occurs because libraries are not randomly assigned to collective bargaining status, but rather employees and library management make explicit choices on the matter. Estimates of the wage and output equations that ignore the underlying choice model will be biased because they will confound the effect of an explanatory variable on wages and output with its effect on the probability that the library's employees are covered by a collective bargaining agreement. To correct for this sample selectivity problem requires us to model the underlying economic choice process that determines whether a library's employees are unionized. This problem is complicated by the fact that such an event is a product of both employee and employer decisions.

To keep our estimation problem manageable, we assume that the choice process that determines whether a library's employees are covered by a collective bargaining agreement can be approximated by:

\[(A7) \quad S^*_i = \delta_0 d_{qi} + \delta_1 d_{wi} + \sum_{r=3}^{R} \delta_r z_{ri} + v_i \]

\[U_i = 1 \text{ if } S^*_i > 0 \]

\[= 0 \text{ otherwise} \]
Here $S_i^*$ is an unobserved variable that represents the likelihood that a municipal library will be unionized, $v_i$ is a random error term, and the $Z_{ri}$ are all of the variables expected to influence the probability of observing a collective bargaining agreement, other than $d_{qi}$ and $d_{wi}$. The parameter $\delta_0$ is assumed to be greater than zero, as positive output effects resulting from collective bargaining should reduce employers' opposition to collective bargaining. The sign of $\delta_1$ is indeterminate, however, as positive union/nonunion wage differentials will increase library employees' demand for collective bargaining, but also increase municipal employers' attempts to resist unionization.

Although $S_i^*$ is not observed, we can arbitrarily scale its cut-off value to be zero, so that if $S_i^*$ is greater than zero, the library's employees will be covered by a collective bargaining agreement ($U_i = 1$). Similarly, if the index is less than or equal to zero, the employees would not be covered by an agreement ($U_i = 0$).

Consistent estimates of the model specified in (A1) through (A7) can be obtained using an iterative procedure originally suggested by Lung-fei Lee.* One can substitute the wage and output equations (A2) to (A5) into (A1) and (A7) to obtain a reduced form probit selection model

\[(A10) \quad S_i^* = \sum_{t=1}^{T} B_t X_t^* + n_i\]

*Lung-fei Lee, op.cit.
where the \( X_{t1} \) are all of the predetermined variables in the model \((X, Y, \text{and } Z's)\) and \( u_i \) is a random error term. Now suppose that the error terms from this reduced form selection model and the wage and library output equations are jointly normally distributed with means zero and the following covariance matrix

\[
\begin{bmatrix}
\varepsilon_{11} \\
\varepsilon_{21} \\
\varepsilon_{31} \\
\varepsilon_{41} \\
u_i \\
\end{bmatrix} \sim N
\begin{bmatrix}
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
\end{bmatrix}
\begin{bmatrix}
\sigma_{11} & \sigma_{12} & \sigma_{13} & \sigma_{14} & \sigma_{1n} \\
\sigma_{21} & \sigma_{22} & \sigma_{23} & \sigma_{24} & \sigma_{2n} \\
\sigma_{31} & \sigma_{32} & \sigma_{33} & \sigma_{34} & \sigma_{3n} \\
\sigma_{41} & \sigma_{42} & \sigma_{43} & \sigma_{44} & \sigma_{4n} \\
\sigma_{n1} & \sigma_{n2} & \sigma_{n3} & \sigma_{n4} & \sigma_{nn} \\
\end{bmatrix}
\]

Under these assumptions one can show that

\[
\begin{align*}
(A12) \quad & E(\log W_{ui} | X_{ji}, U_i = 1) = \sum_{j=1}^{K} \alpha_{ju} X_{ji} \\
& + (\sigma_{1n}/\sigma_n) \lambda_{1u} + h_{1i} \\
(A13) \quad & E(\log W_{ni} | X_{ji}, U_i = 0) = \sum_{j=1}^{K} \alpha_{jn} X_{ji} \\
& + (\sigma_{2n}/\sigma_n) \lambda_{1n} + h_{2i} \\
\text{and} \\
(A14) \quad & E(\log Q_{ui} | Y_{ji}, U_i = 1) = \sum_{j=1}^{M} B_{ju} Y_{ji} \\
& + (\sigma_{3n}/\sigma_n) \lambda_{1u} + h_{3i} \\
(A15) \quad & E(\log Q_{ni} | Y_{ji}, U_i = 0) = \sum_{j=1}^{M} B_{jn} Y_{ji} \\
& + (\sigma_{4n}/\sigma_n) \lambda_{1n} + h_{4i}.
\end{align*}
\]
Here the $h_i$ are normally distributed random variables with mean zero and the $\lambda_i$ are given by

\[
(A16) \quad \lambda_{iu} = \phi\left(-\frac{\sum_{t=1}^{T} B_t X_{ti}^*}{\sigma_n}\right) / [1 - \phi\left(-\frac{\sum_{t=1}^{T} B_t X_{ti}^*}{\sigma_n}\right)]
\]

\[
\lambda_{in} = -\phi\left(-\frac{\sum_{t=1}^{T} B_t X_{ti}^*}{\sigma_n}\right) / \phi\left(-\frac{\sum_{t=1}^{T} B_t X_{ti}^*}{\sigma_n}\right)
\]

where $\phi(\cdot)$ denotes the normal probability density function and $\phi$ the corresponding distribution function.

Equations (A12) through (A16) make it clear why OLS estimates of the underlying wage and output equations (A2) through (A5) may lead to biased estimates. As long as the error terms in the wage or output equations are correlated with the error term in the reduced form selection rule ($\sigma_{1n} \neq 0$, $\sigma_{2n} \neq 0$, $\sigma_{3n} \neq 0$, $\sigma_{4n} \neq 0$) OLS estimates will be biased due to an omitted variable. While $\lambda_{iu}$ and $\lambda_{in}$ are not directly observed, estimates of them may be obtained by first estimating the reduced form probit selection model (A10) obtaining estimated coefficients ($B_t/\sigma_n$), and then using these estimates to compute predicted values $\hat{\lambda}_{iu}$ and $\hat{\lambda}_{in}$ for each individual. Lee (1978) shows that estimation of (A2) to (A5) by OLS, with $\hat{\lambda}_{iu}$ ($\hat{\lambda}_{in}$) added as an additional explanatory variable, over a sample of libraries that are covered by (not covered by) a collective bargaining agreement, will lead to consistent estimates of the $\alpha_ju$ and $B_ju$ ($\alpha_jn$ and $B_jn$). Consequently, consistent estimates of the estimated wage and output differentials associated with collective bargaining coverage may be obtained from (A6).