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CEO Pay-For-Performance Heterogeneity Using Quantile Regression

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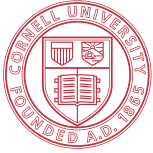
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WORKING PAPER SERIES

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Working Paper 08 – 07



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This paper has not undergone formal review or approval of the faculty of the ILR School. It is intended to make results of Center research available to others interested in preliminary form to encourage discussion and suggestions.

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Abstract

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JEL: M52, J33, G3

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CEO Pay-For-Performance Heterogeneity Using Quantile Regression

1. Introduction

This paper uses quantile regression as introduced in Koenker and Bassett (1978) to investigate heterogeneity in the relationship between CEO pay and firm performance. There have been hundreds of papers published on executive compensation in the past 20 years in economics, finance, human resource management, and accounting. A great deal of these have focused on the relationship between the compensation of the top manager and the size of the firm or between the compensation of the top manager and the performance of the firm. Most, however, have focused on the estimated *mean* relationship. This paper will use some examples to show that the mean returns mask substantial heterogeneity in the CEO pay and firm performance relationship.

Murphy's (1985) work helped start a surge of interest in this area. Jensen and Murphy (1990) found that CEO wealth changes were only weakly related to firm value changes, and the link was probably too low to provide meaningful management incentives. Hall and Liebman (1998) showed that since stock options are such an important part of managerial pay, the value of options are obviously related to firm value, and there is a link between managerial pay and firm performance.

Most of the important research on the pay versus firm performance relationship has been concentrated on the conditional *mean* effect. Some researchers have considered median regression (e.g., Aggarwal and Samwick, 1999) but most are still fundamentally interested in "central tendency" effects. Others, like Conyon and Schwalbach (2000), have explicitly pointed out that there may be a different pay-for-performance sensitivity for each firm. Baker and Hall (2004) and Schaefer (1998) have made important contributions to the relationship between firm

size and pay-for-performance sensitivities (as detailed below). However, they do not employ quantile regression to document heterogeneity.

We take a much different approach by explicitly using quantile regression to examine the relationship between the compensation of the top manager and the performance of the firm. The main question we seek to answer is: Does the pay-for-performance relationship differ across the conditional distribution of wages of top managers? That is, do conditionally (predicted) high-wage managers have a stronger relationship between pay and performance than conditionally low-wage managers? Although the focus of this work is to document empirical heterogeneity, we also consider some different reasons and explanations for why heterogeneity may exist in pay-for-performance sensitivities and assess whether our results coincide with these explanations. Further work could consider heterogeneity in different empirical specifications to disentangle the theories.

2. Managerial pay and firm performance

In this section, we briefly summarize selection of papers on executive compensation as the baseline for our work, focusing on several main areas. First, we consider some of the background literature on firm size and pay and performance for CEOs. Second, we consider some data issues. Third, we consider some empirical specifications for pay and performance. There is substantial disagreement on this in the literature. For purposes of illustration in this paper, we consider two examples: one concerned with firm size and one with firm performance. Fourth, we introduce the idea of considering heterogeneity by using quantile regression. This last issue is explored more deeply in the latter half of the paper.

2.1 Pay and performance¹

Following a great deal of theoretical work in the area of incentive compensation and executive compensation,² a substantial amount of literature on the empirics of executive

¹ This section relies heavily on the introduction to Hallock and Murphy (1999).

compensation started in the middle of the 1980s. Rosen (1992) provides a clear and careful introduction to the theory and empirical work in this area.

An earlier study by Lewellen and Huntsman (1970) , along with many of the earlier authors, examine whether pay is more closely tied with company profits or company size. Using data on the 50 top companies from the early 1940s through the early 1960s, Lewellen and Huntsman (1970) found that company profits are at least as important as revenues for the firms they studied.

Murphy (1985) examined the pay-for-performance sensitivity (i.e., the relation between executive pay and returns to shareholders) using a panel data sample on 73 large manufacturing firms from 1964 through 1981. Although many cross-sectional studies found no relation between executive pay and firm performance, Murphy (1985) showed that simply using firm fixed effects (and therefore looking within firms) reveals a strong and statistically significant link between pay and performance. This was the first paper to make clear the importance of firm fixed effects in the empirical CEO-pay literature. Coughlan and Schmidt (1985) also investigated changes in cash pay and firm performance using data from the 1970s and early 1980s. Like Murphy, they found a positive pay-for-performance link. They went on to show that there is a negative relationship between CEO turnover and company performance.

Jensen and Murphy (1990) found that CEO wealth changes (from a variety of sources) are only weakly related to wealth changes for shareholders of firms. They concluded that the pay-for-performance sensitivity may be too low to provide meaningful incentives for managers.

In an interesting and more recent paper, Schaefer (1998) investigated the dependence of the pay-for-performance sensitivity on the size of the firm. Among his specific findings, the pay-for-performance sensitivity may be inversely proportional to the square root of firm size.

Baker and Hall (2004) went on to consider the large differences in pay-and-performance

² This includes papers by Jensen and Meckling (1976), Holmstrom (1979), Lazear and Rosen (1981), Grossman and Hart (1983), Fama (1980), and Holmstrom and Milgrom (1987).

sensitivities between small and large firms. They showed that a very important feature is the elasticity of CEO productivity with respect to firm size.

Another paper is that of Hall and Liebman (1998) who show the enormous increase in the use of stock options for senior managers over more than two decades. They also document that the relationship between CEO wealth changes and firm performance is very strong, which obviously makes sense because of the recent trend in managerial compensation in the form of stock options.

2.2 CEO pay and pay-for-performance: An empirical specification

Given the hundreds of papers on executive compensation written in the past 20 years, it is startling that there is not some sort of convergence on a standard empirical specification. This may have to do with differences in fields (e.g., Core, 2002; Engel, Gordon, and Hayes, 2002, in accounting), a specific focus on corporate governance (e.g., Weisbach, 1988), or specific issues such as timing (e.g., Hallock and Oyer, 1999). This paper does not focus on the issue of sorting out the set of empirical specifications. Rather, it focuses primarily on one that is well-known and commonly used (Murphy, 1986).

Similar to Murphy (1999), the basic idea is to consider an equation of the following form:

$$\ln(\text{compensation})_{it} = \beta \ln(\text{firm value})_{it} + \alpha_i t + \gamma_i + \varepsilon_{it} \quad (1)$$

where i represents firms and t represents time in years.

There are many other decisions for the researchers to make, such as whether to measure pay in levels or logs and exactly how to measure performance (e.g. should it be lagged). Another consideration in the context of panel data is whether first differences or fixed effects should be used.

In equation (1), we fundamentally seek an estimate of β . However, it is easy to see that an estimate of β from OLS is likely biased due to the fact that $\gamma_i \neq 0$. Suppose for the moment

that γ_i represents the “quality” of the CEO or some other unmeasured (but for the purposes of this discussion, positive) firm or manager characteristic. Then if we ignore γ_i in our estimation of (1), then β will be upward biased.

One way to eliminate this bias due to the unobserved variable γ_i is to “difference” the data. Differencing (1) yields the following:

$$\begin{aligned} \ln(\text{compensation})_{it} - \ln(\text{compensation})_{it-1} &= \beta \ln(\text{firm value})_{it} - \beta \ln(\text{firm value})_{it-1} \quad (2) \\ &+ \alpha_i t - \alpha_i(t-1) + \gamma_i - \gamma_i + \varepsilon_{it} - \varepsilon_{it-1} \end{aligned}$$

If we let Δ represent the change from year to year, this can be re-written as:

$$\Delta \ln(\text{compensation})_{it} = \beta \Delta \ln(\text{firm value})_{it} + \alpha_i(t - (t-1)) + \varepsilon_{it} - \varepsilon_{it-1} \quad (3)$$

Or

$$\Delta \ln(\text{compensation})_{it} = \theta + \beta \Delta \ln(\text{firm value})_{it} + \eta_{it}, \quad (4)$$

where $\eta_{it} = \varepsilon_{it} - \varepsilon_{it-1}$ and $\theta = \alpha_i(t) - \alpha_i(t-1) = \alpha_i$, which is a constant. Equation (4) is exactly Murphy’s (1986) specification. However, the β being estimated can be compared to the coefficient on firm value in equation (1) once the unmeasured effect, γ_i , is removed. This is important for the discussion below.

We investigate the specification in equation (4) below. We additionally want to explore heterogeneity through the use of quantile regression which we begin to discuss in the next subsection but explain more fully, and with empirical examples, in Section II.

2.3 An additional issue

Obviously, there are many ways to consider the pay-for-performance sensitivity using least-squares regression. The point of this paper, however, is to discover whether there is heterogeneity in the pay-for-performance sensitivity *within* a particular empirical specification. This will be done by simply extending the simple empirical model to quantile regression. This

will allow the pay-for-performance sensitivities to vary across the conditional distribution of wages (as explained in more detail below).

There are several possible reasons why heterogeneity in CEO pay-for-performance sensitivities may exist. Suppose, for example, that CEOs have different “ability” (or motivation, organization, etc.) levels such that the marginal return from effort increases with ability. Firms would want to offer incentive-based contracts to high-ability CEOs to maximize effort, and high ability CEOs would want to work for firms offering incentive-based contracts to maximize earnings. However, if costs of effort by managers are constant (or costs decrease with ability), then low-ability CEOs would prefer fixed-wage contracts from firms where the costs of effort outweigh the return from extra effort. This situation would generate heterogeneity in pay-for-performance sensitivities since incentive contracts would differ by the ability level of the CEO, with higher-ability managers having higher pay-for-performance incentives than low-ability managers.

Other examples of sources of heterogeneity in pay-for-performance sensitivities can be derived from a simple principal-agent model as in Murphy (1999). Suppose that firm value is made up of two parts: value created by effort from the CEO and a random noise term. Also suppose that contracts are made up of two parts: a fixed wage portion and a portion that ties pay to performance of the firm. Given this basic structure, and making some simplifying assumptions about utility and costs of effort, several sources of heterogeneity in pay for performance sensitivities can be explored. Differences in risk across firms (in this case, variance of returns) will lead to heterogeneity, with more risky firms showing smaller pay-for-performance sensitivities than less risky firms. Another source of heterogeneity is the difference in risk aversion across managers, with more-risk averse CEOs tending to have smaller pay-for-performance sensitivities than less-risk averse CEOs. This paper mainly focuses on empirically documenting heterogeneity in the pay-performance link and not in testing alternative theories.

3. Quantile regression basics and the start of our empirical specification

This section provides a brief introduction to quantile regression.³ It is also designed to help avoid a common pitfall in thinking about quantile regression by describing what quantile regression is *not*. In the third sub-section, we describe why quantile regression may be so useful in the context of executive compensation.

3.1 An example of something that is not quantile regression

We have encountered some confusion over the interpretation of and how to implement quantile regression. The example below of a mistaken interpretation illustrates potential problems. First, consider the top left plot in Figure 1, which is simply a plot of Log Compensation and Log Assets for 1,633 CEOs using EXECUCOMP data (described in more detail below) for the year 2004. It also plots the slope of the OLS regression line of Log Compensation on Log Assets through the data.

In this example, we take the data on the compensation of 1,633 CEOs and their assets from the top left plot in Figure 1. We then break the data into five separate groups by sorting on the dependent variable (the data are simply grouped into 5 subsets based on the level of the dependent variable -- e.g., 10% of the sample with the smallest level of CEO compensation, then 10% of the sample with the level of CEO compensation from 20%-30%, then 10% of the sample with the level of compensation from 40%-50%, the 10% of the sample with the level of CEO compensation from 60%-80% and finally 10% of the sample with the level of CEO compensation from 90%-100%, and so on). We then run five separate Ordinary Least Squares Regressions of Log Compensation on Log Assets. This is potentially interesting if one is concerned with only those CEOs earning a particular level of wages. However, it is *not* quantile regression. In fact, this sort of truncating on the dependent variable could lead to misleading results, as is clear below.

³ See Koenker and Hallock (2001) for an introduction to quantile regression.

Reading the rest of Figure 1 from left to right, the 2nd through the 6th graphs represent the five subsets of the data as truncated on the dependent variable. Within each graph, an OLS regression line is fitted through the data. It is clear from the second graph in Figure 2 that the simple relationship between pay and firm size for the lowest 10% of CEOs (in terms of pay) is barely positive. It is also clear that for the highest 10% of CEOs (in terms of pay), the relationship between Log Pay and Log Assets is more strongly positive. This information is summarized in the final plot in Figure 1, which graphs the slope of the least squares line against each of the five pay-level groups. While potentially interesting for certain subsets of the data, this is *not* quantile regression.

3.2 What is quantile regression?

We now turn to a simple discussion of quantile regression. When a CEO is at the τ th percentile (or quantile) of compensation in his industry, a fraction $(1 - \tau)$ of CEOs in the industry are paid more than he is. If he is at the 5th percentile, 95% of CEOs are paid more; if he is at the median, then only half are paid more. Koenker and Bassett (1978) extended these ideas to conditional quantile functions, where quantiles of the conditional distribution of the dependent variable are expressed as functions of the observed independent variables.

Standard OLS regression is used to obtain estimates for the conditional mean of some variable, given some set of covariates. One drawback of this approach is that the estimate obtained is only one number used to summarize the relationship between the dependent variable and each of the independent variables. In particular, this method assumes that the conditional distribution is homogenous. This would imply that no matter where you analyze the conditional distribution, the estimates of the relationship between the dependent variable and the independent variable are assumed to be the same.

Figure 1
Least squares fit on unconditional subsets of the response variable

These panels highlight that quantile regression is *not* ranking the data by levels of the dependent variable and then running separate regressions. The top left figure contains 1,633 observations of Log total CEO compensation plotted against Log Assets from the year 2004. An OLS regression line is plotted through the data. In the next five panels, the data are simply grouped into 5 subsets based on the level of the dependent variable (e.g., 10% of the sample with the smallest level of CEO compensation, then 10% of the sample with the level of CEO compensation from 20%-30%, then 10% of the sample with the level of CEO compensation from 40%-50%, the 10% of the sample with the level of CEO compensation from 60%-80% and finally 10% of the sample with the level of CEO compensation from 90%-100%, and so on). The data “rises” as the figures are read left to right and down. In each of these five panels there is an OLS regression line plotted through the data. The final panel (bottom left) shows the slopes from the previous five plots in the figure. Compensation includes salary, bonus, and the value of options granted (at the time of the grant and according to Black-Scholes). The data are from Standard and Poor’s EXECUCOMP.

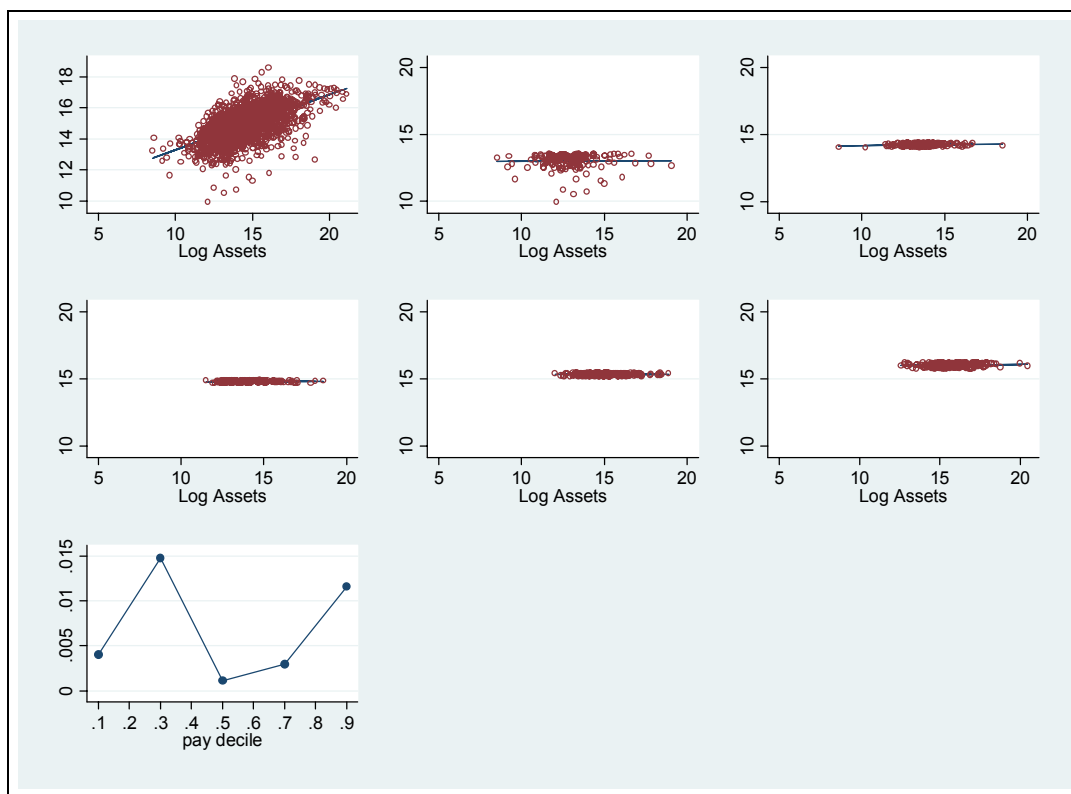
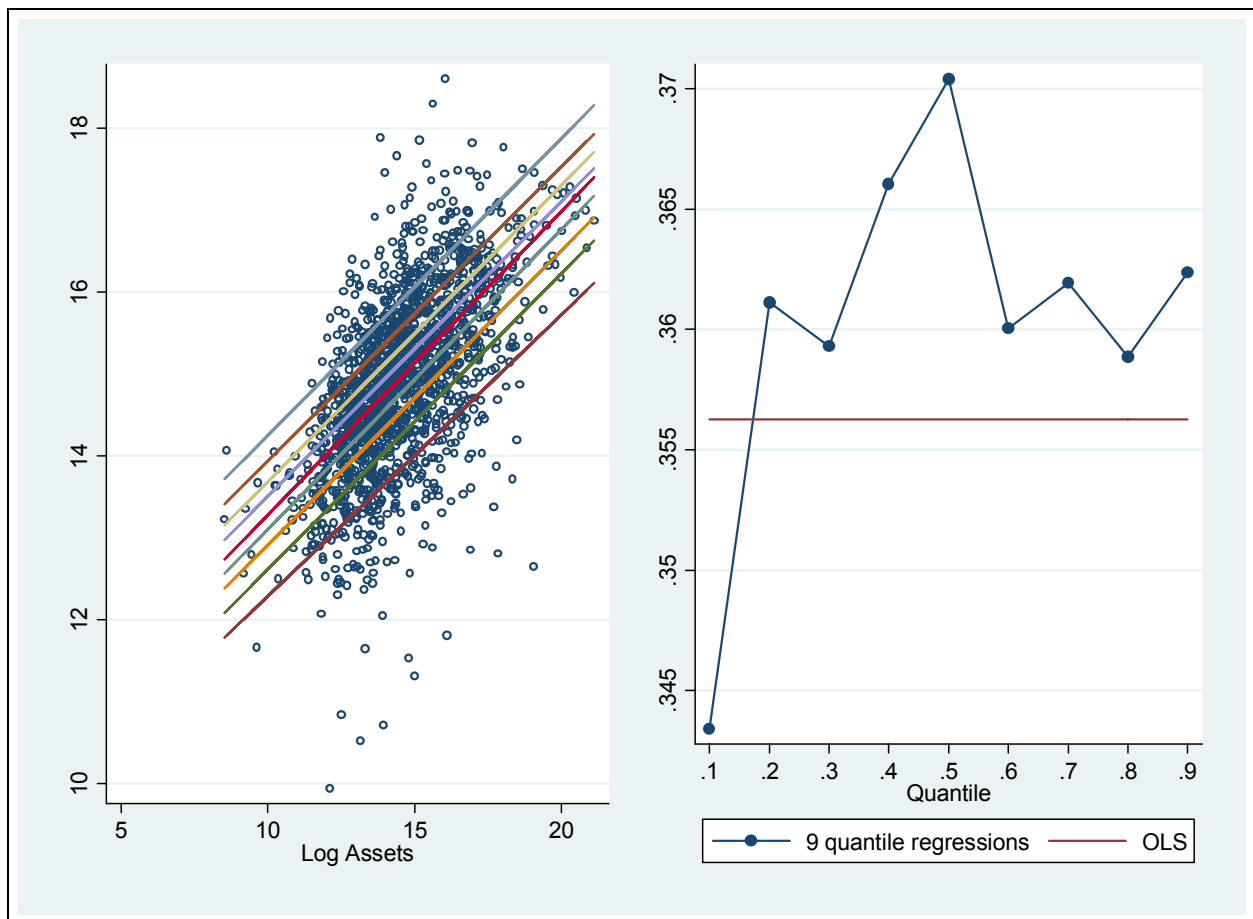


Figure 2
Quantile regressions of log compensation on log assets

The left-hand panel contains 1,633 observations of Log total CEO compensation plotted against Log assets from the year 2004. Quantile regression lines from nine quantile regressions (at 0.10, 0.20, 0.30, 0.40, 0.50, 0.60, 0.70, 0.80, and 0.90) are plotted through the data in the left-hand panel of the figure (the 10th quantile is the bottom line all the way up to the 90th which is the top line). The right-hand figure depicts the nine slopes on Log Assets from the nine quantile regressions, along with the least squares line (horizontal). Compensation includes salary, bonus, and the value of options granted (at the time of the grant and according to Black-Scholes). The data come from Standard and Poor's EXECUCOMP.



Quantile regression, on the other hand, allows for different estimates to be calculated at different points on the conditional distribution. In other words, no assumptions about the homogeneity of the conditional distribution are needed in quantile regression and, in fact, quantile regression can be used to show that the conditional distribution may not be homogenous. If estimates at different quantiles are found to be significantly different from one another, then the conditional distribution is not homogenous.

To be more explicit about the differences between quantile regression and OLS regression, recall that for OLS, we minimize the following with respect to β :

$$SSE = \sum_{i=1}^n (y_i - X_i' \beta)^2 \quad (5)$$

where y is the dependent variable (in our case the log of CEO total annual compensation), X is a matrix of covariates, and β is a vector of coefficients. This will give the standard estimates for the conditional mean of y given X .

Quantile regression minimizes not the sum of squared errors, but rather an asymmetrically weighted sum of absolute errors. Specifically, minimized as:

$$\sum_{i=1}^n |y_i - X_i' \beta(\tau)| \cdot [(\tau)I(y_i > X_i' \beta(\tau)) + (1 - \tau)I(y_i \leq X_i' \beta(\tau))] \quad (6)$$

where y is the dependent variable, X is a matrix of covariates, β is a vector of coefficients which now depends on τ , the quantile being estimated (e.g., $\tau = 0.5$ is the median), and the function I is an indicator function that takes the value of 1 if the condition in the parentheses is true and 0 otherwise. The formula in equation (6) gives weight τ to any observations that are above their respective predicted values and $1 - \tau$ weight to any observations that are below their respective predicted values. This is the same as saying that positive residuals are given weight τ and negative residuals are given weight $1 - \tau$. A special case of this function is conditional median regression where $\tau = 0.5$, since equation (6) collapses to minimizing:

$$\sum_{i=1}^n |y_i - X_i' \beta| \quad (7)$$

which is the standard method for conditional median regression.

Using equation (6), one can estimate $\beta(\tau)$ for any given level of τ between 0 and 1.

Thus, we are not making the assumption that estimates at all points on the conditional

distribution are the same (as in OLS) since estimates for $\beta(\tau)$ explicitly depend on the point of the conditional distribution being estimated (τ).

To reiterate, quantile regression is not the same as dividing the data into different percentiles (or groups) and then running OLS on each percentile. Cutting the data in this way and then calculating separate estimates means that not all of the data are being used for each estimate (since only the data from a given group will be used). For each quantile regression estimate, all of the data are being used. However, some observations get more weight than others.

We can see that quantile regression is a simple extension of the analysis already presented in Figure 1. In the top left plot in Figure 1, we graphed a single OLS regression line through the simple cross-section of data from the year 2004 as follows:

$$\ln(\text{compensation})_i = \beta \ln(\text{assets})_i + \varepsilon_i \quad (8)$$

and our estimate of $\hat{\beta} = 0.377$. There has been a long history of literature on this simple relationship between log compensation for managers and log firm size. This literature has always assumed that there was *one* return to firm size (e.g., Rosen, 1992). Quantile regression helps us consider if the return might vary along the conditional distribution of wages. In a simple quantile regression case, we extend this as follows:

$$\ln(\text{compensation})_i = \beta_\tau \ln(\text{assets})_i + \varepsilon_i$$

where we can estimate separate $\hat{\beta}_\tau$ for any particular quantile. In the case of Figure 2, we do this for $\tau = 0.10, 0.20, 0.30, 0.40, 0.50$ (the median regression), $0.60, 0.70, 0.80$, and 0.90 .

Although the corresponding quantile regression lines in the left panel of Figure 2 look very

similar, they are not exactly so. In fact, $\hat{\beta}_{\tau=0.10} = 0.343$, $\hat{\beta}_{\tau=0.20} = 0.361$, $\hat{\beta}_{\tau=0.30} = 0.359$, $\hat{\beta}_{\tau=0.40} = 0.366$, $\hat{\beta}_{\tau=0.50} = 0.370$, $\hat{\beta}_{\tau=0.60} = 0.360$, $\hat{\beta}_{\tau=0.70} = 0.362$, $\hat{\beta}_{\tau=0.80} = 0.359$, and $\hat{\beta}_{\tau=0.90} = 0.362$. These coefficients are plotted against their respective quantiles (along with the horizontal OLS

estimate) in the right-hand panel of Figure 2. Clearly, the slopes increase sharply as we go from the 0.10 quantile up to the median, and then decline as we go further in the conditional distribution of wages. The horizontal line in the right-hand panel of figure 2 represents the OLS estimate. It is clear that there is substantial heterogeneity around this estimate.

3.3 Why use quantile regression now and in this context?

Quantile regression may be particularly useful in this context for several reasons. First, there is a great deal of heterogeneity in the levels of and changes in compensation across firm types. Similarly, there is wide variation in firm size, however measured, even within the EXECUCOMP sample used here and described below. This is one of the chief reasons for the confusion over the standard empirical specification for thinking about CEO pay and firm performance. Second, although the techniques of quantile regression have existed for some time, there is now rapid growth in applications. Finally, other researchers (e.g., Schaefer, 1998; Conyon and Schwalbach, 2000; Baker and Hall, 2004) have shown that there are some differences in pay for performance sensitivities by different firm characteristics (e.g., firm size).

Quantile regression will allow us to use *all* of the data at once and to consider whether there is heterogeneity in the pay-and-performance relationship across the *conditional* distribution of wages.

4. The Data

In this section, we describe the data and simple descriptive statistics. The data used here, from Standard & Poor's EXECUCOMP, are now commonly used in the literature on executive compensation.

4.1 Basic data description and positive features

The data used in this work are from Standard & Poor's EXECUCOMP from 1992-2004. There are several useful features of these data. First, the data include detailed information on the compensation of the top five highest paid executives over the thirteen-year period. We

focus our attention on the Chief Executive Officer of each firm. Second, the data set is large and contains information from about 1,500 firms for each of the thirteen years of the sample. Third, since the data contain information from a wide variety of firms (Standard & Poor's 500-stock index, Standard & Poor's Mid-Cap 400, and SmallCap 600 there is considerable variation in firm size which will prove useful.

4.2 Sample descriptive statistics

We consider 17,403 CEO-year observations in the main part of our analysis. Table 1 shows that for the entire sample period, the median CEO had salary and bonus of \$750,000 and total compensation (including the Black-Scholes value of stock options at the time of grant) of \$1,688,000. Median sales in these firms is \$908 Million, and the median market value of equity in the firms is \$1.03 Billion. Descriptive statistics for all variables in each of the years from 1992 – 2004 are also reported in Table 1.

Table 1
Summary statistics, medians

Median statistics for companies and CEOs are reported overall and by year from 1992-2004. Data are presented on salary and bonus, total compensation (including the value of options granted), sales, assets market value and return on assets). All data in table are medians except for sample sizes. Data only include information for CEOs. Samples sizes are for compensation. The data are from Standard and Poor's EXECUCOMP. (a) In thousands. (b) In millions.

	Total	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004
The CEO														
Salary + bonus^(a)	745	483	500	554	576	650	675	672	746	810	810	920	1,008	1,239
Total compensation^(a)	1,688	785	854	968	1,036	1,253	1,460	1,574	1,930	2,186	2,345	2,393	2,424	3,036
The firm														
Sales^(b)	908	599	595	645	707	728	788	834	944	1,053	1,089	1,039	1,136	1,345
Assets^(b)	1,154	943	754	783	852	862	916	993	1,127	1,308	1,381	1,412	1,555	1,818
Market value^(b)	1,027	573	603	578	732	813	1,027	947	1,091	1,176	1,273	1,062	1,493	1,816
Return on assets (%)	3.94	3.67	3.99	4.25	4.18	4.52	4.64	4.01	4.30	4.28	2.91	3.14	3.45	4.25
N	17,403	678	954	1,040	1,118	1,281	1,388	1,474	1,490	1,496	1,530	1,628	1,676	1,630

5. Is there heterogeneity in the pay-for-performance relationship?

Although it is clear from the right-hand panel of Figure 2 that there is heterogeneity in the return to firm size (as measured by assets), this section is specifically focused on considering heterogeneity in the pay-for-performance relationship. We do this by simply extending the model introduced in Section 2.2 to the quantile regression context. We then compute the return across the quantiles of the conditional distribution of compensation for the managers.

5.1 Heterogeneity in Murphy's (1986) specification?

A very well-known specification we investigate is that of Murphy (1986). We have only slightly modified this specification so that the pay-for-performance sensitivity (β) can vary by the quantiles, τ . We denote this in equation (10) as β_τ

$$\Delta \ln(\text{compensation})_{it} = \theta + \beta_\tau \Delta \ln(\text{firm value})_{it} + \eta_{it} \quad (10)$$

Table 2 presents the results from ten different estimates of the pay-for-performance relationship with the change in the natural log of salary and bonus plus the value of options granted in a given year as the dependent variable. The numbers for the quantile regression estimates can be interpreted as conditional on a set of covariates: if a CEO is expected to lie in the τ -th quantile of the wage distribution, then the estimated pay for performance sensitivity equals β_τ .

For example, the coefficient estimate on change in shareholder value in Table 2 for the 10% quantile implies that given the set of covariates, a CEO in the 10th percentile of the conditional wage distribution is expected to have a pay-for-performance sensitivity of -0.0074. It is clear that the OLS ($\beta = 0.0673$) and median regression ($\beta_{\tau=0.50} = 0.0580$) estimates are somewhat similar. However, it is also clear that as the quantiles increase so do the pay-for-performance sensitivities. This is easily seen in Figure 3, which plots each of the ten quantile regression estimates from Table 2 (along with the 95% confidence intervals).

Table 2
Pay for performance sensitivities

OLS and quantile regression estimates are included for the following empirical specification:

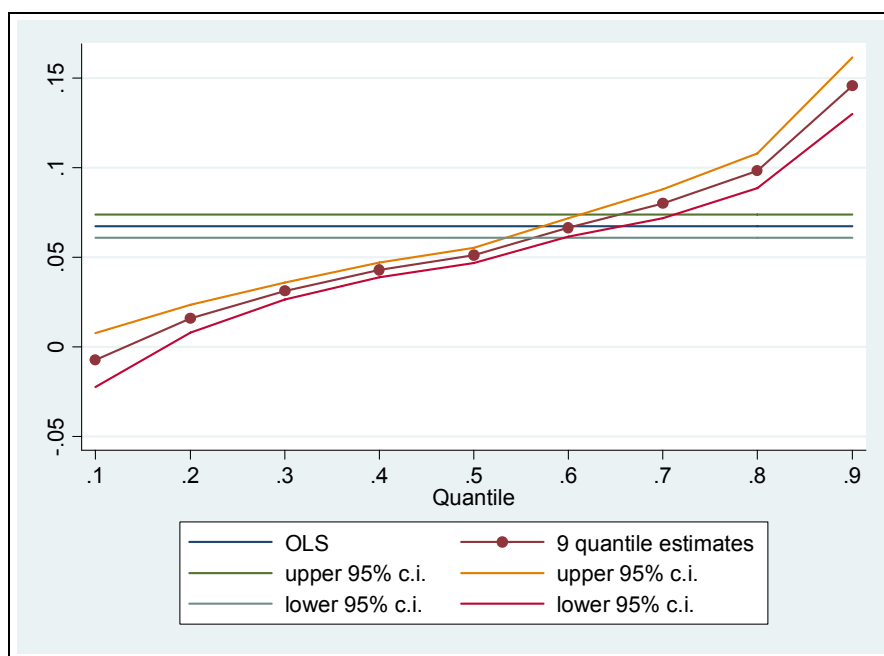
$$\Delta \ln(\text{compensation})_{it} = \theta + \beta_{\tau} \Delta \ln(\text{firm value})_{it}$$

Standard errors are in parentheses. The dependent variable is change in compensation (including salary, bonus, and the value of options granted this period as valued by Black-Scholes). Data are from Standard and Poor's EXECUCOMP, 1992-2004, and only include information on CEOs.

	OLS	$\tau = 0.10$	$\tau = 0.20$	$\tau = 0.30$	$\tau = 0.40$	$\tau = 0.50$	$\tau = 0.60$	$\tau = 0.70$	$\tau = 0.80$	$\tau = 0.90$
$\Delta(\text{firm value})_{it}$	0.0673 (0.006)	0.0074 (0.015)	0.0157 (0.008)	0.0312 (0.005)	0.0429 (0.004)	0.0580 (0.004)	0.0665 (0.005)	0.0799 (0.006)	0.0982 (0.010)	0.1456 (0.016)
R ²	0.0114									
N	9,556	9,556	9,556	9,556	9,556	9,556	9,556	9,556	9,556	9,556

Figure 3
Quantile regression estimates of β_{τ}

The empirical model estimated is $\Delta \ln(\text{compensation})_{it} = \theta + \beta_{\tau} \Delta \ln(\text{firm value})_{it}$. Compensation includes salary, bonus, and the value of options granted (at the time of the grant and according to Black-Scholes). The horizontal lines represent the OLS estimate and the 95% confidence intervals. The dots represent the nine quantile regression estimates and corresponding confidence intervals. Data are from Standard and Poor's EXECUCOMP, 1992-2004.



From this picture we can see that conditionally low-wage CEOs have a smaller pay-for-performance sensitivity than conditionally high-wage CEOs.⁴ If we assume that conditionally high-wage CEOs are typically “higher quality managers,” then these results would suggest that firms tie CEO pay with performance more tightly when the CEO is of higher quality. This could make sense since higher quality CEOs would tend to give the firm high return on their effort. Therefore, inducing higher effort from the CEO by linking pay to firm performance would outweigh the cost to the firm of monitoring CEO effort if the CEO is high quality. These results would also suggest that linking pay to performance for low-conditional-wage CEOs may not be as profitable for the firm for similar reasons. The results in Table 2 would also coincide with the explanation suggested in section I.C, where high ability CEOs have higher pay-for-performance sensitivities than low ability CEOs if ability is positively related to conditional wages. This is likely to be the case but cannot be formally tested in this setting without some measure for ability. In order for these results to match an explanation based on risk aversion, one would have to argue that high-conditional-wage CEOs tend to have lower risk aversion than low-conditional-wage CEOs. Since we doubt that it is the case that risk aversion differs in this way across CEOs, we cannot say whether this explanation for heterogeneity is valid given our results.

The next obvious question is whether the returns to performance differ *significantly* across quantiles. For example, in specification (10), we get $\beta_{\tau=0.10} = -0.0074$ and $\beta_{\tau=0.50} = 0.0580$. The general procedure for hypothesis testing used here to establish a case for heterogeneity is based on the work of Koenker and Bassett (1982) and Hendricks and Koenker (1991). Tests of hypotheses that take the form $H_0: \beta_{\tau_1} = \beta_{\tau_2}$ against $H_1: \beta_{\tau_1} \neq \beta_{\tau_2}$ can be written as:

⁴ This discussion supposes that β measures the relationship between compensation and firm value. This is exactly what equation (10) is doing since (10) is just a variant of (1) with the unobserved fixed effect, γ_i , removed. Differencing as in either (4) or (10) is essentially running a fixed-effects model like (1).

$$T_n = (\hat{\beta}_{\tau_1} - \hat{\beta}_{\tau_2})' (H^{-1} J H^{-1})^{-1} (\hat{\beta}_{\tau_1} - \hat{\beta}_{\tau_2}) \quad (11)$$

where $H^{-1} J H^{-1}$ is the “sandwich” formula used in Hendricks and Koenker (1991). This test has an asymptotic F distribution when it is divided by its degrees of freedom. This form of the test can be used to either test a vector of coefficients across a pair of quantiles or to test a single coefficient across a pair of quantiles. In the case of a single coefficient, this statistic simplifies to:

$$T_n = \frac{(\hat{\beta}_{p,\tau_1} - \hat{\beta}_{p,\tau_2}) - (\beta_{p,\tau_1} - \beta_{p,\tau_2})}{\sqrt{V(\hat{\beta}_{p,\tau_1}) + V(\hat{\beta}_{p,\tau_2}) - 2Cov(\hat{\beta}_{p,\tau_1}, \hat{\beta}_{p,\tau_2})}} \quad (12)$$

where p is the variable of interest and $\beta_{p,i}$ (where $i = 1, 2$) is the coefficient estimate at a given quantile for the variable. This version of the formula may be a bit more intuitive since it looks similar to the standard tests for differences in means. Instead of using this form to test for differences in means, we are using a similar procedure to test for differences in conditional quantile estimates.

These tests can be used to establish a case for heterogeneity because if the null hypothesis is rejected, we can conclude that there are significant differences across quantiles. Given that these differences are significant, this would suggest that there is evidence that the pay-for-performance sensitivity is different at different points in the conditional distribution (i.e., there is significant heterogeneity in pay-for-performance sensitivities across the conditional wage distribution).

Table 3 shows the results of tests for significant differences for all possible cases outlined in Table 2. For example, the F-statistic for testing whether there is a significant difference between $\beta_{\tau=0.1}$ and $\beta_{\tau=0.5}$ is 28.320, which is significant at the 1% level. In fact, all of the coefficients are significantly different from one another. This implies that significant heterogeneity exists in pay for performance sensitivities using the Murphy (1986) specification.

Table 3
F statistics for differences in slopes across quantiles

This table reports F statistics for testing across specifications in Table 2. All combinations are significantly different from one another at the 1% level.

	$\tau = 0.20$	$\tau = 0.30$	$\tau = 0.40$	$\tau = 0.50$	$\tau = 0.60$	$\tau = 0.70$	$\tau = 0.80$	$\tau = 0.90$
$\tau = 0.10$	6.988	14.628	22.103	28.320	43.685	54.066	80.130	91.950
$\tau = 0.20$	-	13.033	26.541	37.979	69.623	76.116	134.010	100.510
$\tau = 0.30$	-	-	18.221	33.203	78.564	70.455	153.120	88.732
$\tau = 0.40$	-	-	-	17.411	73.810	52.257	147.680	75.269
$\tau = 0.50$	-	-	-	-	59.803	38.341	127.210	65.976
$\tau = 0.60$	-	-	-	-	-	11.379	70.528	48.315
$\tau = 0.70$	-	-	-	-	-	-	19.825	38.540
$\tau = 0.80$	-	-	-	-	-	-	-	22.471

5.2 Relation with other pay-for-performance work

Canyon and Schwalbach (2000) also investigate a type of heterogeneity in the pay-for-performance relationship using data from the UK and Germany, but they do not use quantile regression. Instead, the authors estimate a separate pay-for-performance sensitivity for every firm in their data set, and then consider the distribution of those estimates. In other words, they examine the distribution across firms of conditional mean estimates of within-firm pay-for-performance sensitivities. Using our data, we use a similar method in Figure 4 to document the types of differences in sensitivities pointed out by Canyon and Schwalbach in the UK and Germany. We ran specifications like equation (4) (analogous to Figure 3 and Tables 2 and 3) 1,585 times. The 1,585 represents the number of firms for which we have data for three consecutive years. In Figure 4, we plot the distribution of within-firm returns⁵, with 4.2% (median 6.1%) with wide variability.

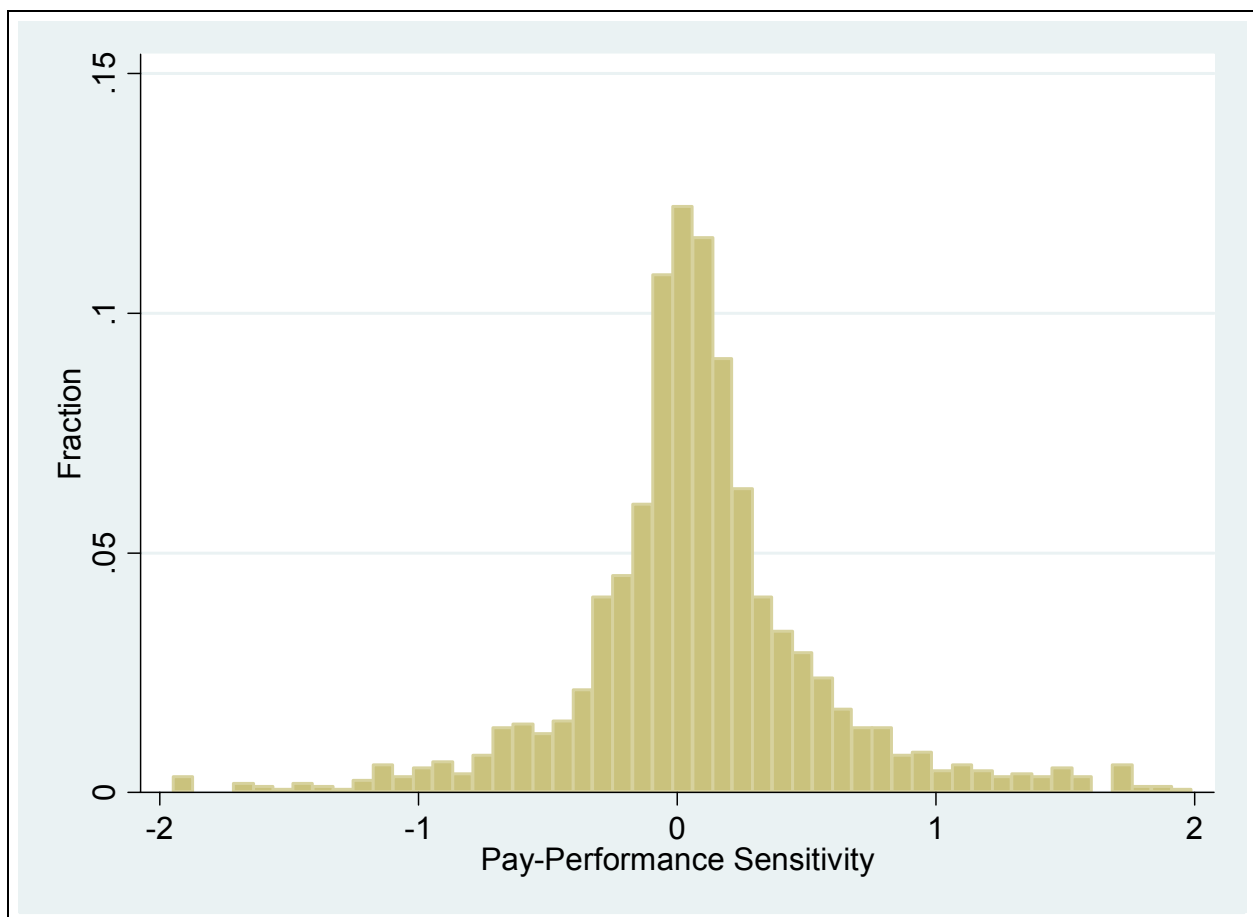
Though our example of the Canyon and Schwalbach (2000) method shows a form of heterogeneity in the pay-for-performance relationship, this is not the same as the heterogeneity shown using quantile regression. The estimates from the quantile regressions used in our

⁵ 2.6% of the returns are outside of the bounds in the figure.

paper suggest heterogeneity in the pay-for-performance sensitivity across the conditional distribution of wages, not across firms, as in Conyon and Schwalbach.

Figure 4
Within-firm OLS regressions of pay-size link

The empirical model estimated is $\Delta \ln(\text{compensation})_{it} = \theta + \beta \Delta \ln(\text{firm value})_{it}$. This is estimated 1,585 times, once for each of 1,585 firms for which we have three consecutive years of data. The histogram in the figure is the graph of each of the 1,585 within-firm $\hat{\beta}$ coefficients. Compensation includes salary, bonus, plus the value of options granted (at the time of the grant and according to Black-Scholes). The data are from Standard & Poor's EXECUCOMP.



Other recent work on the firm size effect and CEO pay include Baker and Hall (2004) and Schaefer (1998). Baker and Hall find that firm size has different effects on different measures of CEO incentives, and they attempt to show under which circumstances each measure of

incentives should be used for analysis. Specifically, they find that if activities have dollar impact that is the same across different firm sizes, then the measure of CEO incentives should be the CEO's "percent owned"; and if activities have percentage returns that are constant across firm size, then the CEO's "equity stake" should be used. Schaefer (1998) develops a model based on agency theory that includes both costs of effort by the CEO and risk aversion and uses this model to examine the effect of firm size on pay-for-performance sensitivities. He finds that pay-for-performance sensitivity is inversely proportional to the square root of firm size, independent of how firm size is measured. Rather than distinguishing among different theories of compensation, our goal is to empirically examine executive pay using quantile regression. Our hope is that quantile regression techniques will ultimately be helpful in contributing to this literature as well.

6. Concluding comments and future work

There is a lot of interesting literature on the economics of executive compensation. Much of this work has concentrated on the relationship between the pay of the top manager and the performance of the firm. Even more recent work has suggested that the relationship between pay and performance in firms is not constant across all firm types (e.g., Schaefer, 1998; Conyon and Schwalbach, 2000; Baker and Hall, 2004).

This paper uses quantile regression techniques developed by Koenker and Bassett (1978) to investigate whether there is heterogeneity in the pay-for-performance link across the conditional distribution of wages for managers of U.S. firms over the years 1992 – 2004. The results suggest that for some commonly used specifications in the literature, there is considerable heterogeneity in returns to firm performance across the conditional distribution of wages. But what is the fundamental source of this heterogeneity? There are several possible sources, such as firm risk, firm beta, managerial ability, managerial risk aversion, and the shape of the firm's age-wage profiles. Each of these is a potential fruitful area for future work.

These ideas can be extended to many other areas. One is in the area of management turnover. The theory of quantile regression has only recently been extended to the case of binary response variables (Kordas, 2000). With this, ideas from the extensive literature on CEO turnover could be explored in the quantile regression context. Another area of interest is relative performance evaluation of CEOs. We expect that quantile regression will continue to be used in these and many other interesting areas.

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